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# A Generic Framework for Connector Architectures based on Components and Transformations

H. Ehrig, J. Padberg, B. Braatz, M. Klein<sup>1</sup>

*Institute for Communication and Software Technology  
Technical University Berlin, Germany*

F. Orejas, S. Perez, E. Pino<sup>2</sup>

*Departament de Llenguatges i Sistemes Informàtics,  
Universitat Politècnica de Catalunya, Barcelona, Spain*

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## Abstract

The intention of this paper is to extend our generic component framework presented at FASE 2002 [4] to a specific kind of connector architectures similar to architectural connections in the sense of Allen and Garlan [1]. In our generic component framework we have considered components with explicit import, export and body parts connected by embeddings and transformations and composition of components with a compositional transformation semantics. Our framework, however, was restricted to components with a single import and export interface. Here we study architectures based on connectors with multiple imports and components with multiple exports. Architectures studied in this paper are built up from components and connectors in a noncircular way. The semantics of an architecture is defined by reduction step sequences in the sense of graph reductions. The main result shows existence and uniqueness of the semantics of an architecture as a normal form of reduction step sequences. Our generic framework is instantiated on one hand to connector architectures based on CSP as the formal specification technique in the approach by Allen and Garlan. On the other hand it is instantiated to connector architectures based on high-level-replacement systems in general and Petri nets in particular. A running example using Petri nets as modeling technique illustrates all concepts and results.

*Keywords:* Components, connector architecture, Petri net transformations

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<sup>1</sup> Email: {ehrig,padberg,bbraatz,klein}@cs.tu-berlin.de

<sup>2</sup> Email: {orejas,sperezl,pino}@lsi.upc.es

## 1 Introduction

The importance of architecture descriptions has become most obvious over the last decade (see e.g. [17,18,7,10,6]). Various formalisms have been proposed to deal with the complexity of large software systems. In order to build up large software systems from smaller parts, a flexible component concept for software systems and infrastructures are a useful and widely accepted abstraction mechanism (see e.g. [19,12,8]). Although there are many approaches available, only few are general enough to be used for different specification techniques. To achieve a generic concept the focus has to be on the fundamental issues of components and component-based systems. These are the interfaces, the compositionality of components and its embedding into the environment.

In our FASE 2002 paper [4] we have presented a generic component framework for system modeling that can be used for a large class of semi-formal and formal modeling techniques. According to this concept a component consists of a body, an import, and an export interface, and connections between import and body as well as export and body. These connections are again generic to allow a great variety of instantiations. We only require having suitable notions of embeddings, called inclusions in [4], and transformations (e.g. refinements) between specifications, such that the import connection of a component defines an embedding and the export connection a transformation. The connection between import and export interfaces of different components are also represented by transformations. In fact, one of the key concepts of our framework is a generic notion of transformations of specifications, especially motivated by - but not limited to - rule-based transformations in the sense of graph transformation and high-level replacement systems [5,2,16]. In this paper we extend our generic component framework discussed above to a specific kind of connector architectures motivated by architectural connections in the sense of Allen and Garlan [1]. In fact, our generic framework in [4] is restricted to components with a single import and export interface. We consider architectures using connectors with multiple imports and components with multiple exports that allow connecting one connector to several different components. The key concept for the corresponding composition of a connector with components is a parallel extension diagram for transformations. This generalizes the notion of an extension diagram in [4] which is the key concept to define transformation semantics for components and to prove compositionality. Architectures studied in this paper are built up from components and connectors in a noncircular way. The semantics of an architecture is defined by reduction step sequences, where in each reduction step one connector is composed with all adjacent components. The main result shows existence and uniqueness of the semantics as a normal form of reduction step sequences.

This paper continues with the construction of the connector architecture in Section 2. In this and the following sections we have an ongoing example using Petri nets. In Section 3 we show the composition of components with connectors. Subsequently we show the existence of a unique semantics for architectures in Section 4. In Section 5 we give a concrete instantiation to CSP and a more abstract instantiation to high-level replacement systems including Petri nets as a concrete case. In Section 6 we conclude with a brief discussion of related work and an outlook to future research.

## 2 Construction of Connector Architectures

In this section we present the main syntactical concepts of our general framework for connector architectures. The framework in [4] as well as the framework in this paper is generic not only concerning the underlying concept of semi-formal or formal specifications, but also concerning the concept of transformations in order to model abstraction and refinement between interfaces and body of one component, or between import and export interfaces between different components. In this section we only require that transformations are closed under composition and that we have a special kind of transformations, called embeddings, which intuitively model inclusion of specifications, and a notion of independence of embeddings explained below. Motivated by architectural connections in the sense of Allan and Garland [1] we distinguish in this paper components and connectors with multiple interfaces, while we have considered only components with single interfaces in [4]. Now a component  $COMP = (B, e_1 : E_1 \Longrightarrow B, \dots, e_n : E_n \Longrightarrow B)$  for  $n \geq 0$  is given by the body  $B$  and a family of export interfaces  $E_i$  with export transformations  $e_i : E_i \Longrightarrow B$  for  $i \in \{1, \dots, n\}$ . A connector  $CON = (B, b_1 : I_1 \rightarrow B, \dots, b_n : I_n \rightarrow B)$  for  $n \geq 2$  is given by the body  $B$  and a family of import interfaces  $I_i$  with body embeddings  $b_i : I_i \rightarrow B$  for  $i \in \{1, \dots, n\}$ . We assume that the family of embeddings  $b_i : I_i \rightarrow B$  for each connector is **independent**. This means intuitively that the import interfaces  $I_i$  of  $B$  are pairwise disjoint. Now we can define formally how a connector connects different components. Given a connector  $CON = (B, b_1, \dots, b_n)$  of arity  $n$ , and  $n$  components  $COMP_i = (B_i, e_{i_1}, \dots, e_{i_{m_i}})$  of arity  $m_i$  with connector transformations  $con_i : I_i \Longrightarrow E_{i_k}$  with  $1 \leq k \leq m_i$  for  $i \in \{1, \dots, n\}$  then we obtain the **connector diagram** in Figure 1 and the **connector graph** in Figure 2:

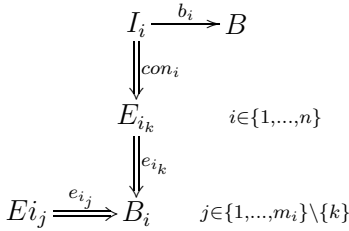


Fig. 1. Connector Diagram

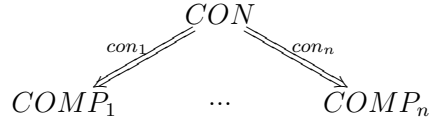


Fig. 2. Connector graph

**Remarks:**

- A connector diagram consists of  $n$  import interface nodes  $I_i$  of  $n + 1$  body nodes  $B_i$  and  $B$ , and of  $\sum_{i=1}^n m_i$  export interface nodes  $E_{i_j}$ , even if some of the specifications may be equal, e.g.  $B_1 = B_2$
- Circular connections as in (2) are forbidden, unless we duplicate the body as in (1) of Figure 3. Otherwise the semantics of such a circular architecture is not defined, as it would cause the identification of the export interfaces  $E_{1_1}$  and  $E_{1_2}$  of component  $COMP_1$  or other kinds of unwanted side effects.

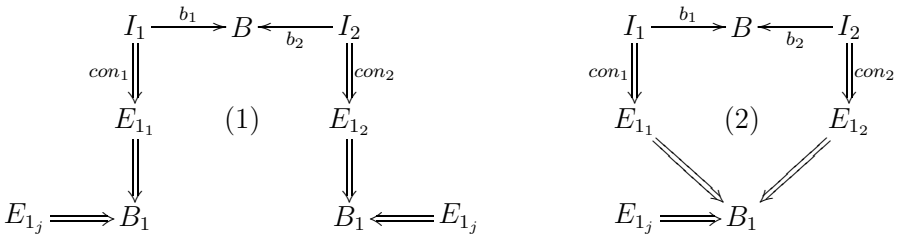


Fig. 3. Noncircular and circular connector diagrams

- A well-known result from graph theory for undirected graphs (i.e. forgetting the direction of the arcs) is that in a connected, noncircular graph the number of nodes exceeds the number of edges by one:  $\#nodes(G) = \#edges(G) + 1$ . In Figure 3 we have  $\#nodes(1) = 9 = \#edges(1) + 1$ , but  $\#nodes(2) = 7 \neq 8 = \#edges(2) + 1$

Now, we introduce the architecture based on connectors and components. Similarly to connectors we obtain an architecture diagram and an architecture graph. The first describes the architecture at the level of specifications and the second as a graph, where nodes are connectors or components.

An **architecture**  $A$  of arity  $(k, l)$  consists of  $k$  components and  $l$  connectors, an architecture diagram  $D_A$  and an architecture graph  $G_A$ : The **architecture diagram**  $D_A$  is a diagram built up from the  $l$  connector diagrams and the connection transformations satisfying the following conditions

- (i) **Connector Condition:** Each import interface  $I$  of a connector is connected by an arrow, labeled with a connection transformation  $con : I \implies$

$E$ , to exactly one export interface  $E$  of one component.

- (ii) **Component Condition:** Each export interface  $E$  of a component is connected at most to one import interface  $I$  of a connector by an arrow from  $I$  to  $E$ , labeled with a connection transformation  $con : I \implies E$ .
- (iii) **Noncircularity:** The architecture diagram  $D_A$  is connected and noncircular aside from the arrows' direction.

The **architecture graph**  $G_A$  of architecture  $A$  is obtained from the architecture diagram  $D_A$  by shrinking each connector diagram in  $D_A$  to the corresponding connector graph. Hence, it consists of nodes labeled by the connectors and components and arrows in between labeled with the corresponding connection transformations.

**Petri Net Example for a Connector Architecture: Preparing a Party**

To provide a concrete example for a connector architecture we have chosen place/transition nets as the underlying specification technique. In Section 5 we discuss the instantiation of connector architectures to Petri nets. The main focus of this simple and small example is to illustrate the introduced concepts, using a scenario from everybody's life: preparing a party. In order to show the Petri nets explicitly, a component is drawn as a rectangular, including one or more rectangulars in the first row, where each contains one export net. The rectangular in the second row contains the body net and the component name. A connector is drawn as a rectangular as well. In the first row we have exactly one rectangular, containing the body. The second row comprises at least two rectangulars, each containing one import net.

The components comprise the following activities: **Comp\_invite** in Figure 4 the invitation of guests and the management of cancellations. The component has merely one export interface **Ei**. The places of the export net are preserved under the transformation, but the transition is replaced by the whole subnet in between the places. In Figure 5 we give the usual diagram for the component **Comp\_invite**, but without the explicit Petri nets.

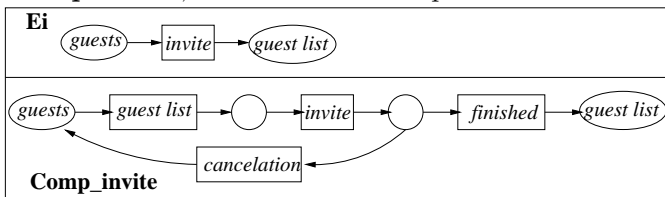


Fig. 4. Component **Comp\_invite**

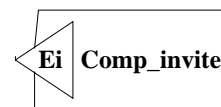


Fig. 5. Classical Diagram

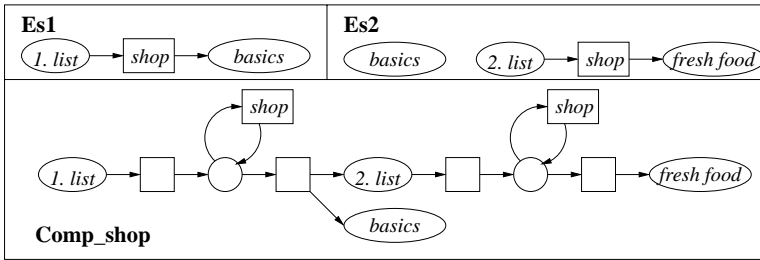


Fig. 6. Component **Comp\_shop**

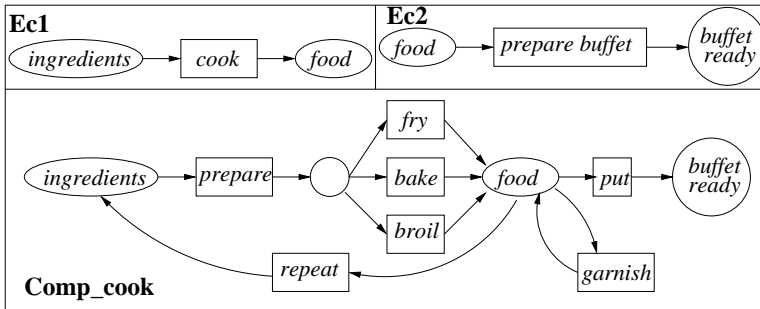


Fig. 7. Component **Comp\_cook**

The component **Comp\_shop** models the shopping, where we assume that the party requires shopping two times sequentially, once for the basics (beverages, potato crisps, olives, etc.) and once for the fresh food (bread, cheese, fruits, etc.). So we have two export nets **Es1**, **Es2** that are transformed into the body net. These transformations keep the places and replace the transition by the subnet in between. The last component **Comp\_cook** comprises the cooking and preparations of the buffet, and provides therefore two export interfaces **Ec1** and **Ec2**.

The connector **Con\_week** in Figure 8 connects the activities that concern the preparations of the week before the party and provides two import nets **Iw1** and **Iw2**. These are mapped by inclusion into the body net. In Figure 9 we give the usual diagram for the connector **Con\_week**, but without the nets.

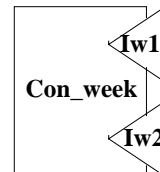
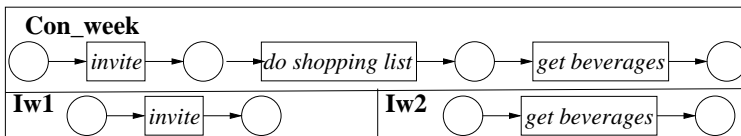


Fig. 8. Connector **Con\_week**

Fig. 9. Classical Diagram

The connector **Con\_day** in Figure 10 connects the preparations on the day of the party, and provides two imports as well.

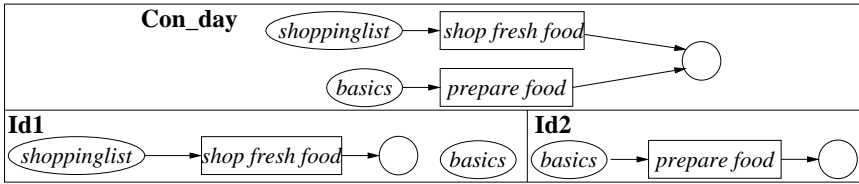


Fig. 10. Connector **Con\_day**

The architecture diagram  $D_A$  is given in Figure 11, where the transformations between the import nets and the corresponding export nets merely rename places or transitions. In Figure 11 we use the names of connectors and components for the corresponding bodies.

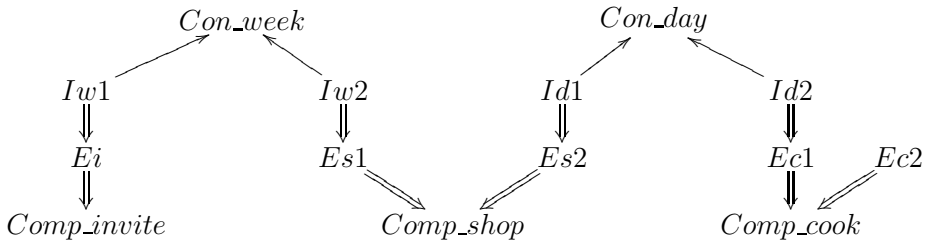


Fig. 11. Architecture diagram  $D_A$

### 3 Composition of Components

In this section we present our concept for the composition of components by a connector, which is the basic step for the construction of the semantics of architectures in the next section. For this purpose we have to require in our generic framework an essential property for embeddings and transformations: The **parallel extension property** is a key concept which generalizes the extension property in [4] from single (sequential) to multiple (parallel) transformations. The intuitive idea is that each family of transformations  $(t_i : SPEC_i \Rightarrow SPEC'_i)_{i \in I}$  can be extended to a parallel transformation  $t : SPEC \Rightarrow SPEC'$ , provided that we have independent embeddings  $b_i : SPEC_i \Rightarrow SPEC'$ . More precisely, the **parallel extension property** means the following: For each family  $(b_i : SPEC_i \rightarrow SPEC)_{i \in I}$  of independent embeddings and for each family of transformations  $(t_i : SPEC_i \Rightarrow SPEC'_i)_{i \in I}$  there is a canonical (parallel) transformation  $t : SPEC \Rightarrow SPEC'$  together with the independent embeddings  $(b'_i : SPEC'_i \rightarrow SPEC)_{i \in I}$  leading to the **parallel extension diagram** (1)

$$\begin{array}{ccc}
 SPEC_i & \xrightarrow{b_i} & SPEC \\
 t_i \Downarrow & (1) & \Downarrow t \\
 SPEC'_i & \xrightarrow{b'_i} & SPEC'
 \end{array}$$

Fig. 12. Parallel extension diagram

in Figure 12. Moreover, parallel extension diagrams are required to be closed

under **vertical composition** and to **include the (classical) extension diagram** in the sense of [4] as a special case where all but one of the transformations  $t_i$  are identical transformations. Now we are able to define the composition of components.

The **composition of  $n$  components by a connector of arity  $n$**  is defined as follows: Given the corresponding connector diagram (see Figure 1) we construct the corresponding parallel extension diagram (1) in Figure 13. The result of the composition of the components  $COMP_1, \dots, COMP_n$  by the connector  $CON$  with the connection transformations  $con_1, \dots, con_n$  is again a component

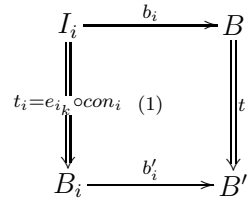


Fig. 13. Composition

$COMP = (B', (e'_{ij} : E_{ij} \implies B')_{ij \in I \times J})$  with  $e'_{ij} := b'_i \circ e_{ij} : E_{ij} \implies B'$  for each  $ij \in \{1, \dots, n\} \times (\{1, \dots, m_i\} \setminus \{k\}) = I \times J$ . In this case we say that  $e'_{ij}$  are extensions of  $e_{ij}$ .

In case of binary components and binary connectors we use the following nice infix notation  $COMP = COMP_1 +_{CON} COMP_2$ . Otherwise we use the notation  $COMP = CON(COMP_1, \dots, COMP_n, con_1, \dots, con_n)$ . The result below can be extended to the composition of connectors with multiple import interfaces.

**Theorem 3.1 (Associativity of Binary Component Composition)**

Given an architecture  $A$  with binary components and binary connectors with the architecture graph  $G_A$  in Figure 14, then we have the following associativity law:

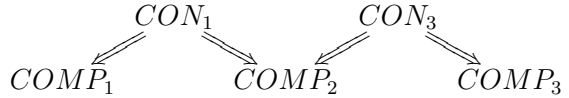


Fig. 14. Binary connectors and components

$$(COMP_1 +_{CON_1} COMP_2) +_{CON_2} COMP_3 = COMP_1 +_{CON_1} (COMP_2 +_{CON_2} COMP_3)$$

**Proof idea:** Each side of the equation can be shown to be equal to a parallel composition of  $COMP_1$ ,  $COMP_2$ , and  $COMP_3$  via  $CON_1$  and  $CON_2$  using the parallel extension property.

**Composition for the Petri Net Example**

Composing first the components **Comp\_invite** and **Comp\_shop** using the connector **Con\_week** we obtain the new component **Comp\_invshop** illustrated in Figure 15.



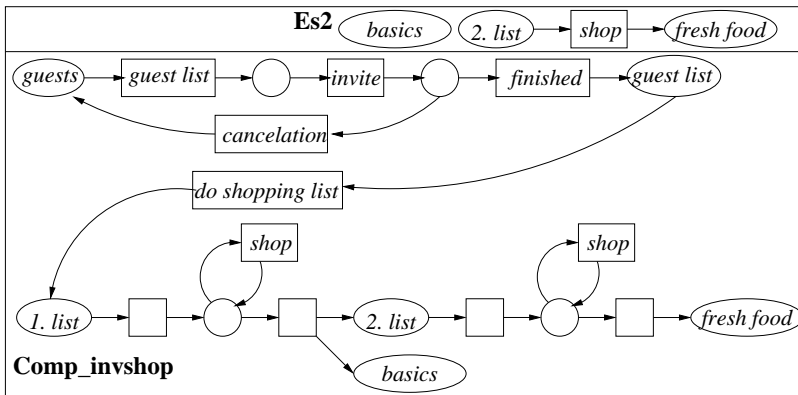


Fig. 15. **Comp\_invshop**

The corresponding parallel extension diagram for the construction of the body  $B'$  of **Comp\_invshop** is depicted in Figure 16, where we again use the names of components or connectors also for their bodies.

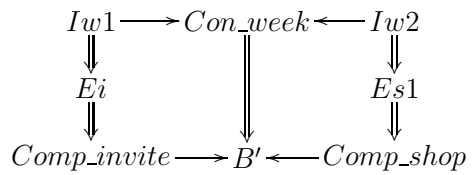


Fig. 16. Parallel Extension diagram

Connecting this component via the connector **Con\_day** with the components **Comp\_cook** we obtain the component **Comp\_invshopcook** in Figure 17. But we can also change the order in which we compose.

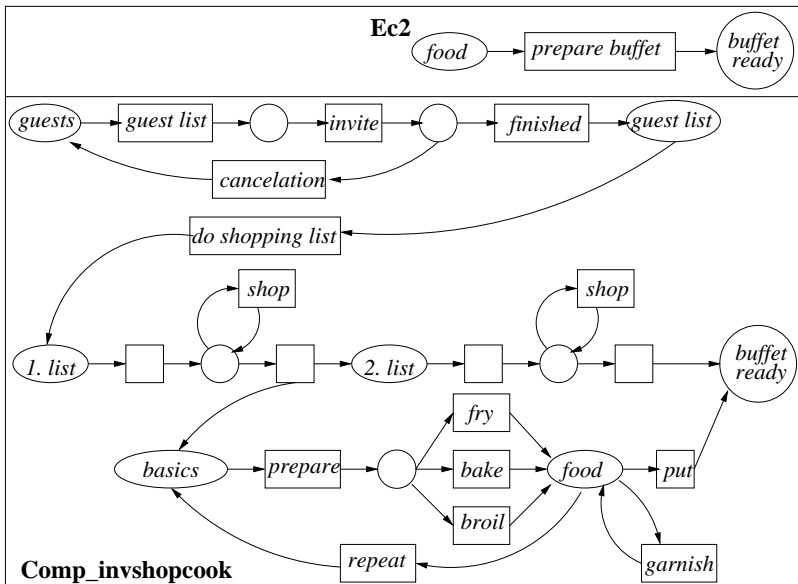


Fig. 17. **Comp\_invshopcook**

So, using the connector **Con\_day** we first compose the components **Comp\_shop** and **Comp\_cook**. Connecting this one via the connector **Con\_week** with the component **Comp\_invite** we again obtain the component **Comp\_invshopcook** in Figure 17. This commutativity is ensured by Theorem 3.1.

### 4 Semantics of Architectures

In this section we define the semantics of architectures. In fact, we construct a well-defined single component as semantics, which corresponds to the composition of all components using all connectors of the given architecture. More precisely, for an architecture there are **reduction rules** that visualize step by step the composition of components via connectors. Both reduction rules are productions  $p = (L \leftarrow K \rightarrow R)$  in the sense of the

algebraic approach to graph transformation [5]. A derivation step in this approach is given by two pushout diagrams (1) and (2) in Figure 18, written  $G \Longrightarrow H$  via  $(p, m)$ , where  $m : L \rightarrow G$  is a graph morphism, that represents the match of  $L$  in  $G$ . Intuitively, we remove  $(L - K)$  from  $G$  in step 1 leading to the context graph  $D$  in (1). And then we add  $(R - K)$  leading to the result  $H$  in (2). The pushout property of (1) and (2) means intuitively that  $G$  is the gluing of  $D$  and  $L$  along  $K$  in (1), respectively  $H$  is the gluing of  $D$  and  $R$  along  $K$  in (2).

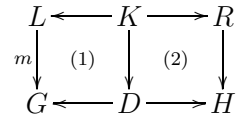


Fig. 18.  $G \Longrightarrow H$

Given an architecture  $A$  with the architecture diagram  $D_A$  and the architecture graph  $G_A$  there is for each connector  $CON$  the following **diagram reduction rule**  $CON_D$ :

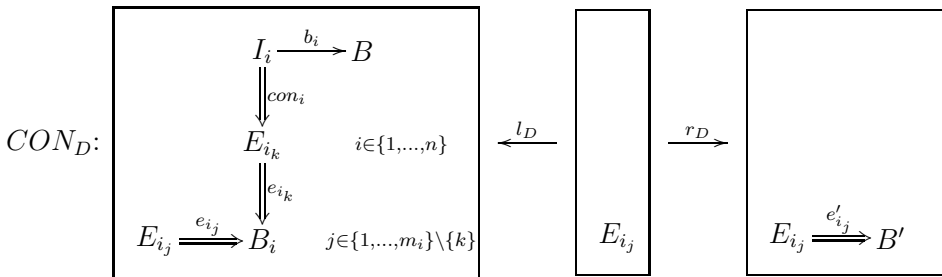


Fig. 19. Diagram reduction rule

where  $B'$  and  $e'_{i_j} = e_{i_j} \circ b'_i$  is defined by the composition:

$$\begin{aligned}
 COMP &= CON(COMP_1, \dots, COMP_n, con_1, \dots, con_n) \\
 &= (B', (e'_{i_j} : E_{i_j} \Longrightarrow B')_{ij \in I \times J}) \\
 &\quad \text{for each } ij \in \{1, \dots, n\} \times (\{1, \dots, m_i\} \setminus \{k\}) = I \times J.
 \end{aligned}$$

The corresponding **graph reduction rule**  $CON_G$  is given in Figure 20 where  $COMP_1, \dots, COMP_n$  are mapped to  $COMP$ . So, a reduction step  $CON_D : D_A \Rightarrow D_{A'}$ , respectively  $CON_G : G_A \Rightarrow G_{A'}$  is given by a derivation step at the level of architecture diagrams, respectively architecture graphs.

For both derivation steps we have inclusions for the matches. Note that  $r_G$  is neither injective nor label-preserving, nevertheless for the reduction rule  $CON_G : G_A \Rightarrow G_{A'}$  the labels of  $G_{A'}$  are well-defined by  $G_A$  and  $COMP$ .

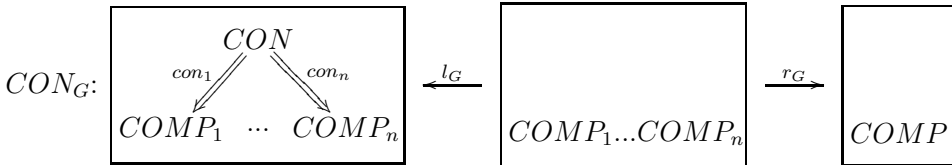


Fig. 20. Graph reduction rule

We can show by an **Architecture Reduction Lemma** that an **architecture reduction rule**  $CON = (CON_D, CON_G)$  reduces an architecture  $A$  to a well-defined smaller architecture  $A'$  with  $D_{A'}$  and  $G_{A'}$  as defined above. The application of  $CON$  is denoted by  $A \xrightarrow{CON} A'$ .  $A'$  is smaller than  $A$  in the following sense: If  $A$  is of arity  $(k, l)$  we can show that  $A'$  is of arity  $(k - n + 1, l - 1)$ , if  $CON$  has arity  $n$ . This means: Given an architecture  $A$  consisting of  $k$  components and  $l$  connectors we obtain the architecture  $A'$  with  $k - n + 1$  components and  $l - 1$  connectors.

Now we can give the **semantics of an architecture** as the result of as many reduction rules as possible. The semantics of an architecture  $A$  is any component  $COMP$  obtained by a sequence of architecture reduction steps  $A \xrightarrow{*} COMP$  from  $A$  to  $COMP$ . The main result given in Theorem 4.1 shows that this semantics always exists and is unique. The main reason therefore is given by the Church-Rosser property, stating that any two architecture reduction steps are locally confluent.

**Theorem 4.1 (Existence and uniqueness of architecture semantics)**

For each architecture  $A$  there is a unique component  $COMP$  which is the semantics of  $A$ .  $COMP$  is obtained by any reduction sequence, where connectors of  $A$  are reduced in arbitrary order:

$$A \xrightarrow{*} COMP$$

**Proof idea:** The architecture reduction step sequences have unique normal forms, as they satisfy the Church-Rosser property due to the following reasoning: If the matches of  $CON_1$  and  $CON_2$  in the architecture diagram  $D_{A_0}$  of  $A_0$  are disjoint, then they are independent and we obtain the result by the Church-Rosser Theorem for graph transformations. Otherwise, due to non-circularity of  $D_{A_0}$ , the matches can overlap at most in one component which allows applying Theorem 3.1, respectively an extension with multiple import

interfaces. So, each maximal sequence has length  $n$ , where  $n$  is the number of connectors in  $A$ .

### Semantics of the Petri Net Example

The application of the reduction rule  $D_A \xrightarrow{CONWEEK} D_{A_1}$  that eliminates the connector **Con\_week** results in the architecture diagram  $D_{A_1}$  given in Figure 21. There we have the new component **Comp\_invshop** with one export **Es2**, that is connected as before to the import **Id1** of connector **Con\_day**. The application of  $D_{A_1} \xrightarrow{CONDAY} D_{A_3}$  that eliminates the connector **Con\_day** yields then the semantics of  $A$ . This is the component **Comp\_invshopcook** in Figure 17 with only one export left, namely **Ec2**. Theorem 4.1 ensures that this semantics exists uniquely. If we start for example with the application of  $D_A \xrightarrow{CONDAY} D_{A_2}$  that eliminates the connector **Con\_day** we obtain a component **Comp\_shopcook** with the two exports **Es1** and **Ec2**. The corresponding architecture diagram  $D_{A_2}$  is given in Figure 22. The subsequent application of  $D_{A_2} \xrightarrow{CONWEEK} D_{A_3}$  eliminating the connector **Con\_day** yields then again the component **Comp\_invshopcook**.

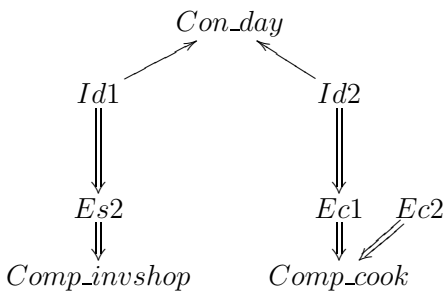


Fig. 21. Architecture Diagram  $D_{A_1}$

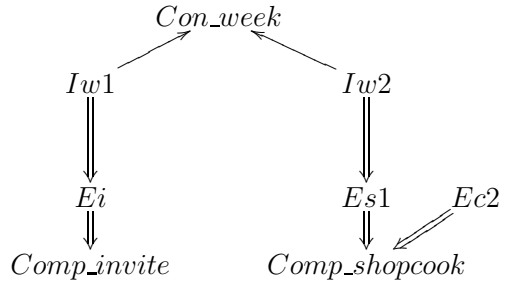


Fig. 22. Architecture Diagram  $D_{A_2}$

## 5 Instantiations

In [1] Allen and Garlan introduced architectural connectors using CSP [9] as specification formalism. In this section we shall very briefly sketch how CSP and Petri nets fit into our transformation framework.

CSP can be seen as an instance of our transformation framework as follows. First, we consider that a CSP specification  $P = (\Sigma, Exp)$  where  $\Sigma$  is a *process signature* (the set of symbols that can be used in  $P$ ) and  $Exp$  is a CSP process expression built over symbols in  $\Sigma$ . Then, we consider that a process  $P$  is embedded in a process  $Q$  if  $P$  is a parallel component of  $Q$ . More precisely,  $P_1 = (\Sigma_1, Exp_1)$  is **embedded** in  $P_2 = (\Sigma_2, Exp_2)$  if  $\Sigma_1 \subseteq \Sigma_2$  and  $Exp_2 \equiv Exp_1 | Exp'$  for some process expression  $Exp'$ .  $P_1$  and  $P_2$  are independently embedded in  $P_3$  iff  $Exp_3 \equiv Exp_1 | Exp_2 | Exp'$  for some process expression  $Exp'$ .

Finally, we consider that transformations are just CSP refinements modulo a signature embedding. This means that a **CSP transformation**  $t: P_1 = (\Sigma_1, Exp_1) \Rightarrow P_2 = (\Sigma_2, Exp_2)$  is an injective mapping  $t: \Sigma_1 \rightarrow \Sigma_2$  such that the translation of  $Exp_1$  through  $t$  satisfies that the failures and divergences of  $Exp_2$  are, respectively, a subset of the failures and divergences of  $t(Exp_1)$ , where  $t(Exp_1)$  denotes the translation of  $Exp_1$  by the renaming of events defined by  $t$ .

Then, CSP can be seen as an instance of our generic approach as a consequence of the **existence of parallel extensions**:

If, for  $i = 1, 2$ ,  $t_i: P_i = (\Sigma_i, Exp_i) \Rightarrow P'_i = (\Sigma'_i, Exp'_i)$  are transformations and  $P_1, P_2$  are independently embedded in  $P_3 = (\Sigma_3, Exp_3)$ , then  $t_3: P'_3 = (\Sigma'_3, Exp'_3)$  is a parallel extension of  $t_1$  and  $t_2$ , where  $\Sigma'_3 = \Sigma_3 + (\Sigma'_1 - t_1(\Sigma_1)) + (\Sigma'_2 - t_2(\Sigma_2))$ , where  $+$  and  $-$  denote disjoint union and set subtraction,  $t_3: \Sigma_3 \rightarrow \Sigma'_3$  is the identity and  $Exp'_3$  is the process expression obtained by substituting  $Exp_1$  by  $Exp'_1$  and  $Exp_2$  by  $Exp'_2$  in  $Exp_3$ .

High-level replacement systems have been introduced in [2] as a generalization of the *Double Pushout* approach for graph transformations from graphs to several kinds of high-level structures in suitable categories including a large variety of different kinds of graphs and Petri nets ([4]). A transformation in the framework of this paper corresponds to a derivation sequence of high-level structures (e.g. Petri nets). The extension property for transformations considered in our general framework for components [4] is well-known as the Embedding Theorem in the theory of high-level replacement systems that holds if a consistency condition between embeddings and transformations is required. A similar consistency condition has to be formulated for the parallel extension property considered in this paper. This property can be shown for high-level replacement systems by considering the Embedding Theorem and the Parallelism Theorem shown in [2]. Moreover, we may allow also some overlapping of the embeddings, provided that the transformations preserve the overlapping part in the sense of parallel independence. This situation occurs for the embeddings of the connector **Con\_day** in Figure 10 in our running example.

## 6 Conclusion

In this paper we have presented a general framework for connector architectures, based on our generic framework for components in [4], and motivated by the architectural connectors approach of Allen and Garlan in [1] which is shown to be a specific instance. It may be mentioned that the papers

[11,20] concerning architecture reconfiguration based on graph transformation techniques can be considered complementary to ours, because graph transformations and high-level replacement play already a fundamental role in our approach.

Future work comprises further and more concrete instantiations especially high-level Petri nets and graph transformation systems. Moreover, larger case studies to evaluate the practical impact are an important task. On the theoretical side the instantiations to general high-level replacement systems has to be worked out in more detail and our framework should be extended to other aspects studied in [4] and architecture reconfiguration in [11,20].

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